### PROGRAMME OUTCOME (PO), COURSE OUTCOME (CO) AND PROGRAMME SPECIFIC OUTCOME (PSO) FOR END SEMESTER STUDENTS UNDERGRADUATE COURSE: 2022-2023

### Programme Name: B. SC. HONS (MATHEMATICS)

#### **PROGRAMME OUTCOMES:**

**PO1: Disciplinary Knowledge** To acquire comprehensive and sufficient knowledge of understanding in Mathematics

**PO2: Critical Reasoning & Problem Analysis:** To acquire the ability of deep study and then critically to think and analyze the subject of mathematics in its different areas.

**PO3: Develop Interdisciplinary Knowledge:** To enable students in developing an effective approach to Interdisciplinary study and enable them to build their own interdisciplinary pathway by choosing courses which make sense to them.

**PO4: Communication skill and attitudes:** Excellent communication of mathematics in geometrical realization, documentation, makes effective presentation develop other branches of sciences, to think existing open programme in mathematics.

**PO5: Self- directed Learning: Ability** to work independently, study the subjects in depth and apply thoughts for solving the problems in various field.

**PO6: Experimental learning and Employability options: Students** are able to identify problems, use constructive reasoning to make viable arguments, and applying mathematics in real-life problems Also they will be able to find job in different sectors of mathematics and mathematics related subjects.

**PO7: Develop Research Related Skill: Capability** of thinking about the various fields of Mathematics advances in those fields and clear concept about them so that appropriate questions are formed on related fields.

## **PROGRAMME SPECIFIC OUTCOME:**

**PSO 1:** Thinking about every topic in a critical manner.

PSO 2: When there arises situation to provide information about any problem students are able to identify it, locate, evaluate and use the information effectively.PSO 3: Realize, evaluate, and formulate different quantitative models arising in socialscience, business and other fields.

**PSO 4:** Apply mathematical and logical arguments to develop and formulate every problem in a unique way.

**PSO 5: Acquire** clear concepts and knowledge to understand every problem and use mathematical and statistical methods by the students through the course.

**PSO 6:** Aware about the responsibility to become a citizen of society and promise to scatter the scope of acquired knowledge.

## Course Outcomes (CO) for End Semester Students: 2022-

## 2023 CO17: (Paper CC13 - Metric Spaces and

### **Complex Analysis**)

CO17:1: Learn the concept of Metric space, Mapping, compactness and Connectedness, Heine-Borel property, contraction, Banach fixed point Theorem related to Metric space.

CO17:2: Concept of various properties of Complex Number, Differentiability andAnalyticity of Complex Valued function, Formation of Cauchy-Reimann equation. Idea about Contour and Contour Integral, Learn related theorem like Cauchy- Goursat theorem and Cauchy Integral formulae.

## CO18: (Paper CC14 – Ring Theory and Linear Algebra-II)

CO18:1: -Study of polynomial rings, division algorithm and consequences.

CO18:2: Idea about dual spaces, dual basis, Cayley-Hamilton theorem and minimal polynomial for a linear operator. Inner product space and its properties. Concept of Least square approximation, Normal and self-adjoint operator, orthogonal projections and Spectral theorem.

# **CO19: (Paper DSE 3 – Number Theory)**

CO19:1: -Learn about linear Diophantine equation, prime counting function, Goldbach conjecture, Chinese Remainder theorem, Fermat's and little son theorem

CO19:2--Concept of Dirichlet's Product, Mobius Inversion formulae, Euler phi function and residues. Learn about integer modulo n, Legendre Symbol, Femat's Last Theorem.

## **CO20:** (Paper DSE4 – Mathematical Modelling)

CO20:1: -Learn Legendre and Bessel's equation and find their power series solution. CO20:2: --Learn about Laplace transform, inverse Laplace transform and its applications to second order PDE and ODE.

CO20:3: --Concept of simulation used in Monte Carlo Simulation Modelling, over viewing optimization modelling, Learn LPP model and use sensitivity analysis.

#### DETAILED SYLLABUS OF END SEMESTER UG (HONOURS) COURSES

#### **DEPARTMENT OF MATHEMATICS**

CC-13: Metric Spaces and Complex Analysis: Credits -06 Content(a)Metric spaces: sequences in metric spaces, Cauchy sequences. Complete metric spaces, Cantor's theorem.

(b) Continuous mappings, sequential criterion and other characterizations of continuity. Uniform continuity. Connectedness connected subsets of R.

Compactness: Sequential compactness, Heine-Borel property, totally bounded spaces, finite intersection property, and continuous functions on compact sets. Homeomorphism. Contraction mappings. Banach fixed point theorem and its application to ordinary differential equation.

(c) Limits, limits involving the point at infinity, continuity. Properties of complex numbers, regions in the complex plane, functions of complex variable, mappings. Derivatives, differentiation formulas, Cauchy-Riemann equations, sufficient conditions for differentiability.

(d) Analytic functions, examples of analytic functions, exponential function, logarithmic function, trigonometric function, derivatives of functions, and definite integrals of functions. Contours, Contour integrals and its examples, upper bounds for moduli of contour integrals. Cauchy- Goursat theorem, Cauchy integral formula.
(e) Liouville's theorem and the fundamental theorem of algebra. Convergence of sequences and series, Taylor series and its examples.

(f)Laurent series and its examples, absolute and uniform convergence of power series.

## C14T: Ring Theory and Linear Algebra II: Credits-06 Course Content

(a) Polynomial rings over commutative rings, division algorithm and consequences, principal ideal domains, factorization of polynomials, reducibility tests, irreducibility tests, Eisenstein criterion, and unique factorization in Z[x]. Divisibility in integral domains, irreducible, primes, unique factorization domains, Euclidean domains.

(b) Dual spaces, dual basis, double dual, transpose of a linear transformation and its matrix in the dual basis, annihilators. Eigen spaces of a linear operator, diagonalizability, invariant subspaces and Cayley-Hamilton theorem, the minimal polynomial for a linear operator, canonical forms.

(c) Inner product spaces and norms, Gram-Schmidt orthogonalization process, orthogonal complements, Bessel's inequality, the adjoint of a linear operator. Least squares approximation, minimal solutions to systems of linear equations. Normal and self-adjoint operators. Orthogonal projections and Spectral theorem.

# DSE -3: (Anyone from the three) Credits 06

**DSE-3A:** Mechanics

OR DSE-3B: Number Theory OR DSE-3C: Industrial Mathematics

# **DSE-4: (Anyone from the three)**

Credit: 06

DSE-4A: Mathematical Modeling

OR

DSE-4B: Differential Geometry

OR

DSE-4C: Bio- Mathematics

|        | PO1 | PO2 | PO3      | PO4 | PO5 | PO6 | PO7 | PSO<br>1 | PSO2 | PSO<br>3 | PSO4 | PSO<br>5 | PSO6 |
|--------|-----|-----|----------|-----|-----|-----|-----|----------|------|----------|------|----------|------|
| CO17.1 | ~   | ~   | ~        | ~   | >   |     | ~   | ~        | ~    |          | ~    |          |      |
| CO17.2 | ~   | ~   | ~        | ~   | ~   |     | ~   | ~        | ~    |          | ~    |          |      |
| CO18.1 | ~   | ~   |          |     | ~   |     | ~   | ~        | ~    |          | ~    |          |      |
| CO18.2 | ~   | ~   | ~        |     | ~   |     | ~   | ~        | ~    |          | ~    |          |      |
| CO19.1 | ~   | ~   |          |     | ~   |     | ~   | ~        |      |          | ~    |          |      |
| CO19.2 | ~   | ~   | ~        |     | ~   |     | ~   | ~        | ~    |          | ~    |          |      |
| CO20.1 | ~   |     | ~        |     | ~   | ~   | ~   |          |      | ~        |      | ~        |      |
| CO20.2 | ~   |     | <b>v</b> |     | ~   | ~   | ~   |          |      | ~        |      | ~        |      |
| CO20.3 | ✓   | ~   | <b>v</b> | ~   | ~   |     | ~   |          |      | ~        |      | ~        |      |

#### MAPPING OF CO, PO, PSO

#### JUSTIFICATION MATRIX OF CO WITH PO & PSO (High: 3, Medium: 2, Low: 1)

|        | Mapping | Correlation | Justification  |
|--------|---------|-------------|--|
| CO17.1 | PO1     | HIGH        | Students will acquire sufficient knowledge about basics of metric spaces.  |
|        | PO2     | HIGH        | Students will be able to learn how to analyze the problem critically and solve the problem.  |
|        | PO3     | HIGH        | Students will learn to understand the behavior of differentiability of different domains (real and complex) and relate another subject like Physics. |
|        | PO4     | MODERATE    | Students can think in advance about topics related to this subject and apply various methods in the real field.                                      |
|        | PO5     | MODERATE    | Students able to analyze the problem on fixed point related with metric space and can be handle by independently.                                    |
|        | PO7     | MODERATE    | Students will be able to identify and formulate the problems of metrics space in a unique Way.   |
|        | PSO1    | HIGH        | Student will acquire the knowledge for critical analysis different problem.  |
|        | PSO2    | HIGH        | Information of various property of metric space will help to identify the connectedness, compactness of metric space                                 |
|        | POS4    | MODERATE    | Students will gather knowledge logically to solve the problem.   |
| CO17.2 | PO1     | HIGH        | Students will be able to obtain vast knowledge on Cauchy-Riemann equation  |
|        | PO2     | HIGH        | Students learn about the questioning on differentiability, C-R equation  |
|        | PO3     | HIGH        | Student will have capability to solve various problem related to it in different field of science.   |
|        | PO4     | MODERATE    | Students will think the topics of contour integral C-R equation etc. In a critical manner  |
|        | PO5     | MODERATE    | Students apply the knowledge of differentiability, Contour integration, in a self-direct way.  |
|        | PO7     | HIGH        | There are so many research problems in this field. So student will be encouraged to pursue themselves into research field.                           |
|        | PSO1    | HIGH        | Students will acquire knowledge to think different complex problem in critical manner.   |

|        | PSO2 | MODERATE | Students realize how to evaluate the problem by figures and models.  |
|--------|------|----------|--|
|        | PSO4 | LOW      | Students will be able to analyze complex problems and acquire clear concepts to handle those.  |
| CO18.1 | PO1  | HIGH     | Students obtain a vivid knowledge on polynomial Ring, consequences   |
|        | PO2  | HIGH     | Acquire knowledge of questioning and reasoning on Ring theory  |
|        | PO5  | HIGH     | Student will identify the problems and solve them using constructive reasoning on this course.   |
|        | PO7  | MODERATE | This course will help student as a gateway to do research on Number theory.  |
|        | PSO1 | HIGH     | Students will acquire knowledge to think different problem in critical manner on polynomial ring and division algorithm                    |
|        | PSO2 | MODERATE | Students will share this knowledge to find out the gcd of two numbers.   |
|        | PSO4 | MODERATE | Students will think and solve the problem logically.   |
| CO18.2 | PO1  | HIGH     | Students learn the concept of ideal, dual space, inner product space.  |
|        | PO2  | HIGH     | Acquire knowledge of questioning and reasoning on ideal, dual spaces, etc.   |
|        | PO3  | MODERATE | Students apply their knowledge of various problems from ideal, dual space perspective.   |
|        | PO5  | MODERATE | Students will be able to think about critical problems related to this course independently.   |
|        | PO7  | HIGH     | Students learn to identify the problems and analyze to find information correctly in this Course.  |
|        | PSO1 | HIGH     | Student will acquire knowledge on advance linear algebra.  |
|        | PSO2 | MODERATE | Students will share their knowledge to identify and solve various type of problem of advance linear algebra.                               |
|        | PSO4 | MODERATE | Student will be able to identify and formulate the problems of dual spaces, inner product space in a unique way                            |
| CO19.1 | PO1  | HIGH     | Learn vividly about conjecture, Fermat's theorem, prime counting etc.  |
|        | PO2  | HIGH     | To understand how to make appropriate questions and reasoning in number theory   |
|        | PO5  | HIGH     | Students learn to understand the problem using concepts of different aspects of this course.   |
|        | PO7  | MODERATE | Students will be able to think about critical problems related to this course.   |
|        | PSO1 | MODERATE | Students realize how to evaluate the problem by figures and models of this course.   |
|        | PSO2 | MODERATE | Students will be able to identify and formulate the problems of number theory space in unique way.   |
|        | POS4 | LOW      | Students will learn logical way to use Chinese Remainder theorem, Fermat's theorem and Diophantine equation.                               |
| CO19.2 | PO1  | HIGH     | Obtain knowledge on Mobius Inversion, residues, Dirichlet's product  |
|        | PO2  | HIGH     | Acquire knowledge about critical reasoning and questioning in Mobius Inversion, residues   |
|        | PO3  | MODERATE | Students learn to communicate with other using concept of different aspect of this course  |
|        | PO5  | HIGH     | Student able to think in advance topics related this subject and improve research skill  |
|        | PO7  | HIGH     | Students learn to identify the problems and analyze to find information correctly in this course   |
|        | PSO1 | HIGH     | Student will be able to identify and formulate the problems of metric space in a unique way  |
|        | PSO2 | LOW      | Knowledge of different method of number theory will be shared by students to various problem of different related field like Cryptography. |
|        | PSO4 | MODERATE | Student will acquire knowledge on this filed to solve the problem using mathematical method and logic.                                     |
| CO20.1 | PO1  | HIGH     | Learn Legendre, Bessel's equation and their power series efficiently   |
|        | PO3  | HIGH     | Students make questioning and reasoning to enrich in specific subject  |
|        | PO5  | MODERATE | Students apply the knowledge of differentiability, Contour integration, in self-directed way.  |
|        | PO6  | MODERATE | Students will be able to think critical problems related to this course  |

|        | PO7  | HIGH     | Students learn to identify the problems and analyze to find information correctly in this course that enables them towards research mind.   |
|--------|------|----------|---|
|        | PSO3 | MODERATE | This method will be very helpful to student for forming various model on Social science, Business and other fields of science.  |
|        | PSO5 | LOW      | Student will be able to create awareness and scope of applying this course  |
| CO20.2 | PO1  | HIGH     | Acquire knowledge on Laplace transform & its application on ODE, PDE  |
|        | PO3  | HIGH     | Students make questioning and reasoning to enrich in LT & its application on ODE, PDE   |
|        | PO5  | MODERATE | Students able to find their scope of job real life problem learning application of this course  |
|        | PO6  | MODERATE | Students will be able to use research methods for this specified course.  |
|        | PO7  | HIGH     | Students will be able to think of critical problems related to Laplace and Inverse LT.  |
|        | PSO3 | MODERATE | This method will be very helpful to student for forming various model on Social science, Business and other fields of science.  |
|        | PSO5 | LOW      | Students realize to evaluate the problem of this course by mathematical & statistical method.   |
| CO20.3 | PO1  | HIGH     | Obtain clear concept on Simulation, sensitivity analysis etc.   |
|        | PO2  | MODERATE | Students make questioning and reasoning to enrich in subject of this course.  |
|        | PO3  | HIGH     | Students apply the knowledge of LPP, Simulationetc. in self-directed way.   |
|        | PO4  | MODERATE | Student able to think in advance topics related this subject and improve research skill   |
|        | PO5  | MODERATE | Students learn to identify the problems and analyze to find information correctly in this course.   |
|        | PO7  | HIGH     | Different optimization technique of this course will be helpful to student for various research problem related to different applied field of science.                              |
|        | PSO3 | MODERATE | This method will be very helpful to student for forming various model on Social science, Business and other fields of science.  |
|        | PSO5 | MODERATE | Student will acquire the knowledge vividly to understand different problem to build a robust model using mathematical method and testifying it robustness using statistical method. |